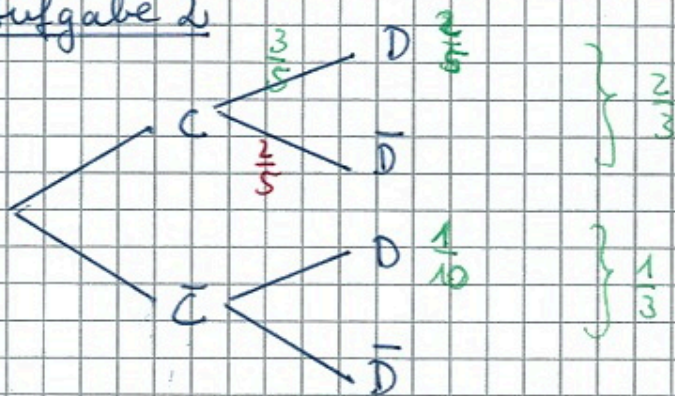


Aufgabe 1

siehe A1

Aufgabe 2



a)
$$P(\bar{D}) = P(C \cap \bar{D}) + P(\bar{C} \cap \bar{D})$$
$$= 1 - P(C \cap D) - P(\bar{C} \cap D)$$
$$= 1 - \frac{2}{5} - \frac{1}{5} = \frac{5}{5} - \frac{3}{5} = \frac{2}{5}$$

b) zu zeigen: $P(C \cap D) \neq P(C) \cdot P(D)$

$$P_C(D) = \frac{P(C \cap D)}{P(C)} \Rightarrow P(C) = \frac{P(C \cap D)}{P_C(D)} = \frac{\frac{2}{5}}{\frac{2}{3}} = \frac{3}{5}$$

$$P(D) = 1 - P(\bar{D}) = \frac{1}{2}$$

$$P(C) \cdot P(D) = \frac{3}{5} \cdot \frac{1}{2} = \frac{3}{10} \neq \frac{2}{5} = P(C \cap D) \text{ q.e.d.}$$

c) ges: $P(\bar{C} \cap D)$

$$P(C \cap D) = \frac{2}{5}$$

$$P_C(D) = \frac{3}{5} = \frac{P(D \cap C)}{P(C)} = \frac{\frac{2}{5}}{P(C)} \Rightarrow P(C) = \frac{2}{3}$$

$$P(C) \cdot P(D) = P(C \cap D)$$

$$\frac{2}{3} \cdot P(D) = \frac{2}{5} \Rightarrow P(D) = \frac{\frac{2}{5}}{\frac{2}{3}} = \frac{3}{5}$$

$$P(D) = P(D \cap C) + P(D \cap \bar{C}) = \frac{2}{5} + P(D \cap \bar{C}) = \frac{3}{5}$$
$$\Rightarrow P(\bar{C} \cap D) = \frac{1}{5}$$